

$$R(s) = G_c(s) + G(s)$$

$$H(s)$$

II classical Controllers (traditional)

*PID => balance between PD &PI.

* Phase-lag = the same as PI.

* Phase-lead \$ " " " The PD.

* Phase clead-lag => " " PID.

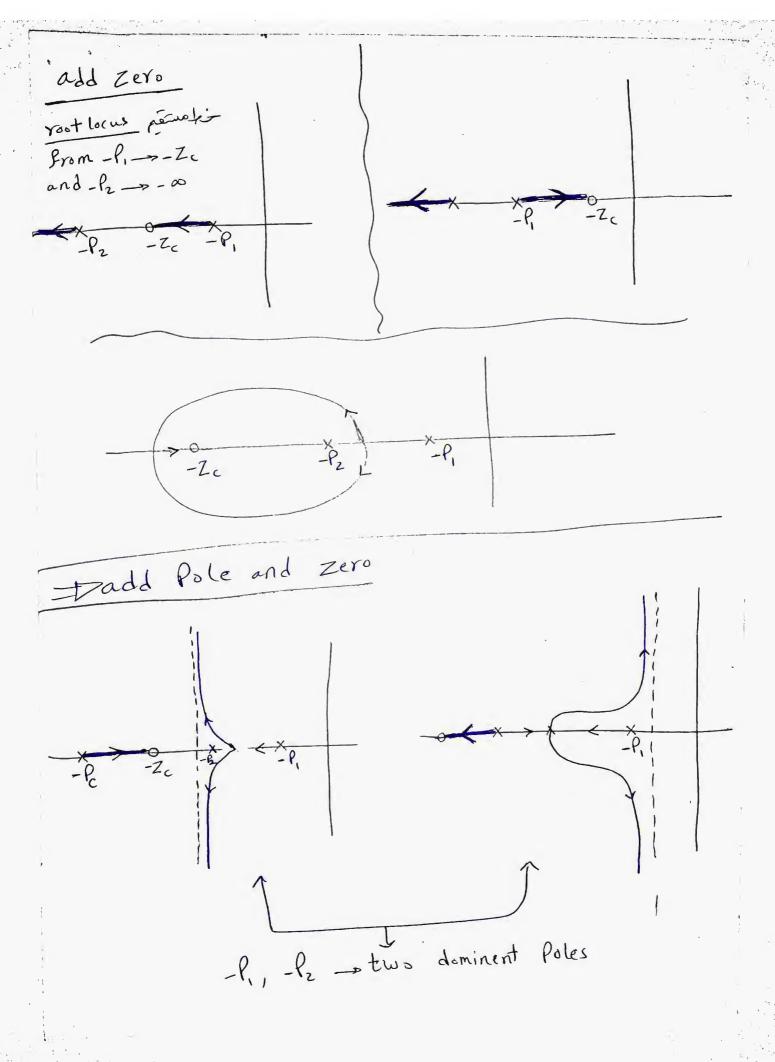
Lec 7 is sur long the sead controller

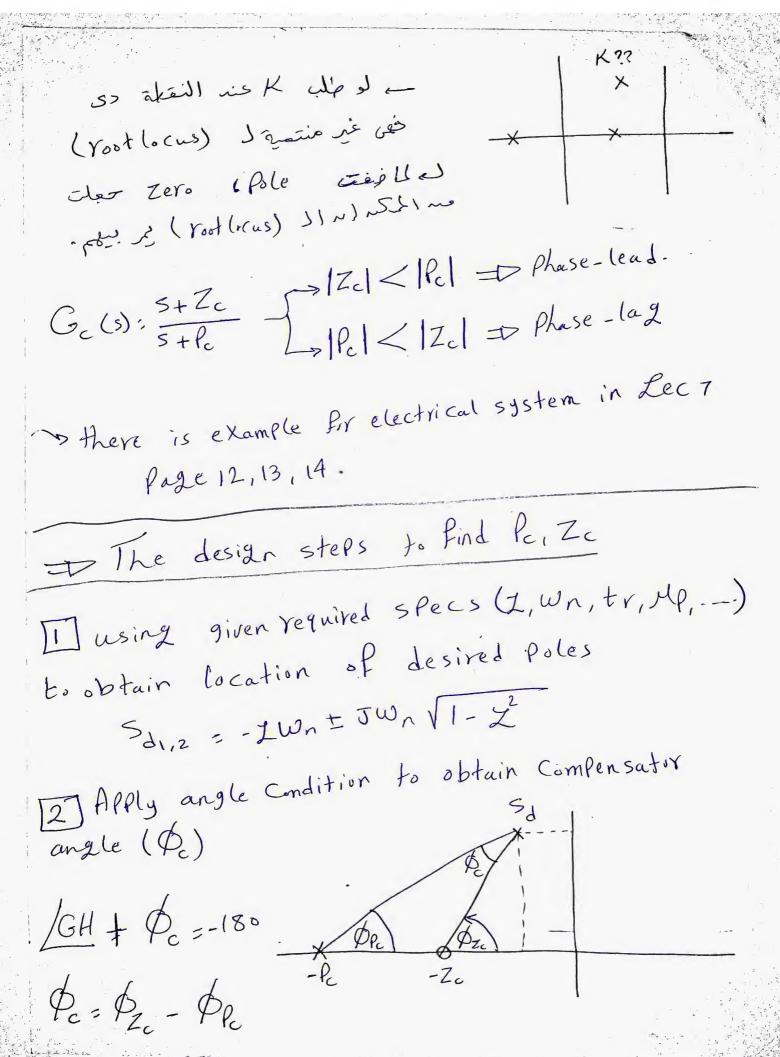
Phase-lead controller

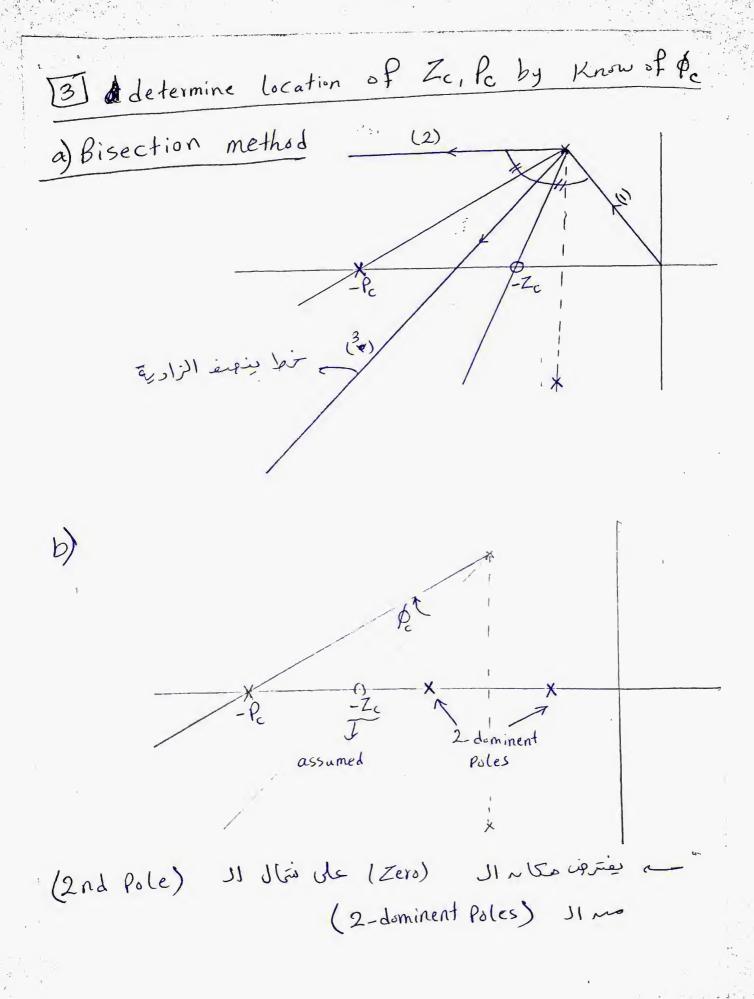
Phase-lead controller

Property

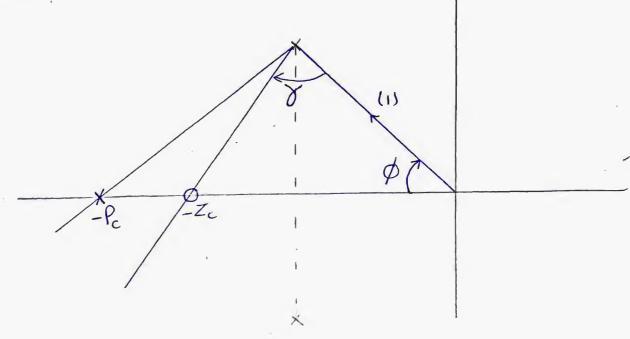
P







[C] Max. attenuated ration , p= Cos 1 8=== [T-p-Pc]



A "in design steps"

Apply magnitude Condition to determine the Value of gain K to meet desired specs:

| K Gc(s) GH(s) | = 1

for checking steady-state error (ess)

DLead Compensator

Laby adding Pole & Zero to the system

* lag Compensator design

i) calculate

Kc: desired value of dc Qain

Kun: System value of dc Qain

2) Assume Zero location (Zc) in range of 10%. From the 2nd diminent Pole of the Sys

$$P_{c} = \frac{Z_{c}}{B}$$
 $K_{dc} = \frac{Z_{c}}{Z_{c}/B} = B$
 $T_{of controller}$

(state space)

x(+)= A x(+) + B u(+)

y(t): c x(t) + 0 u(t)

= . p(ill appropriéte (T.F) il em cres les que D=0

Anxn=bsystem matrix (Bnx1=E ilp matrix

CIXN = Olp matrix X(t) nx1 = State vector

Canonical forms for state space

III Controllable form.

Por 3rd order system T.F = Y(s) s b12+b25+b3

3+a12+a25+a3

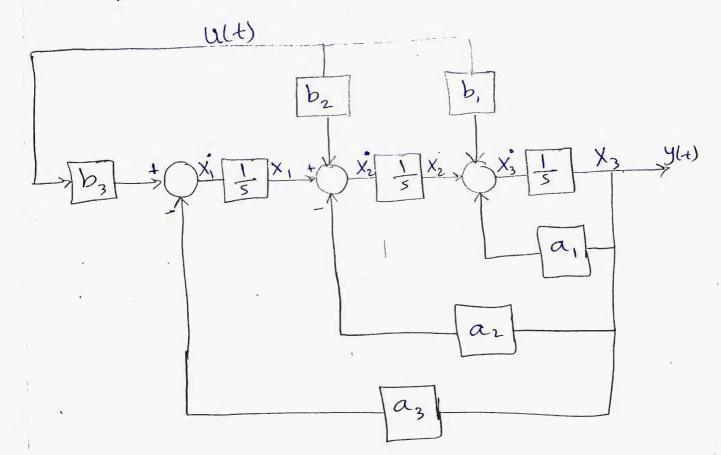
a) V(s) $b_1 s + b_2 s + b_3$ v(s) $b_1 s + b_2 s + b_3$

-> كملها هتوجل للجيفونات.

طريقة معتوره (ط Pirst check that T.F: bis+b25+b3 Ceff. of 3=1 3 + a,2 + a25 + a3 أكرأس ك $\begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_3 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_3 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_3 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_3 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_3 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0$ ع معاملات المعام بإشارة محكومه. $y(t) = (b_3 b_2 b_1) x_1$ x_2 x_3 x_4 x_2 x_3 x_4 x_5 x_4 x_5 x_4 x_5 x_6 x_7 x_8 x_8 لكم بنفس الإشارة. - dill eler i egt om (State) vil(11P) موجوده يكوم النظام (Cntrollable)

$$T.F = \frac{b_1 s^2 + b_2 s + b_3}{s^3 + a_1 s^2 + a_2 s + a_3}$$

$$x(t) = \begin{pmatrix} 0 & 0 & -a_3 \\ 1 & 0 & -a_2 \\ 0 & 1 & -a_1 \end{pmatrix} x(t) + \begin{pmatrix} b_3 \\ b_2 \\ b_1 \end{pmatrix} u(t)$$



$$\frac{if}{T.f} = \frac{b_1s^2 + b_2s + b_3}{s^3 + a_1s^2 + a_2s + a_3}$$

$$\frac{X(s)}{V(s)} = \frac{b_1 s^2 + b_2 s + b_3}{(s+P_1)(s+P_2)(s+P_3)} = \frac{A_1}{s+P_1} + \frac{A_2}{s+P_2} + \frac{A_3}{s+P_3}$$

$$y(s) = \begin{cases} \frac{U(s) - A_1}{(s + P_2)} + \frac{U(s) - A_2}{(s + P_2)} + \frac{U(s) - A_3}{(s + P_3)} \end{cases}$$

$$X_{1}(s) = \frac{U(s)}{s+l_{1}} = DU(s) = (s+l_{1}) \times (s)$$

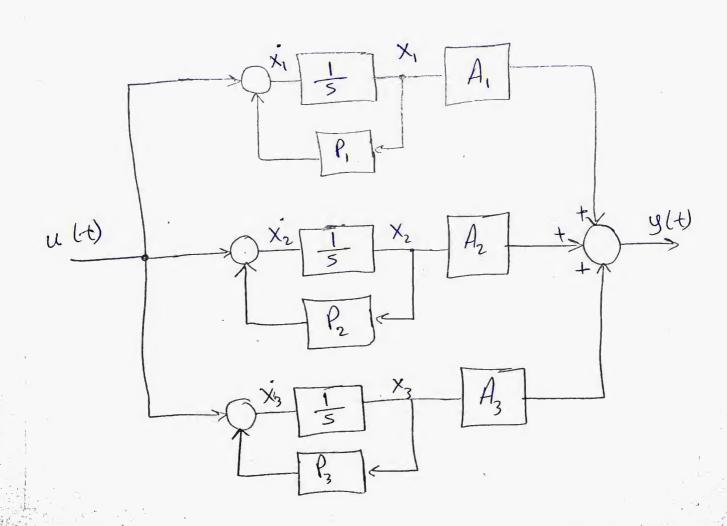
$$X_{1} = -P_{1} X_{1} + U(t)$$
; $X_{2} = -P_{2} X_{2} + U(t)$

$$X_{3} = -P_{3} \times_{3} + u(t)$$

$$\dot{\chi}(t) = \begin{bmatrix} -P_1 & 0 & 0 \\ -P_2 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 \\ 1 \end{bmatrix} \times \begin{bmatrix} 1 \\ 1 \end{bmatrix} \times \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$Y(s) = A_1 \times_1 (s) + A_2 \times_2 (s) + A_3 \times_3 (s)$$

 $Y(t) = A_1 \times_1 (t) + A_2 \times_2 (t) + A_3 \times_3 (t)$
 $Y(t) = (A_1 A_2 A_3) \times (t) \longrightarrow (1)$



State-slace Analysis

Ziven

X = AX+Bu

9 , CX

ے تعاصل النقطات الثلاثة القادمة في المحافرات.

II T.F

T.F = V(S) = e(SI-A) B

2 ch- equation

SI-A = 0 . (system) 11 as la

3 system response to ilp utt)

if x(0) =0 = x(1+) = A x(+) + B u(+) \ L.T

SX(s) = AX(s) = BU(s) + X(o)

(SI-A) X(s) = X(0) + BU(s)

X(s)= (SI-A) x(0) + (SI-A) BUS(S)

Let = O(s) = (SI-A) = transition matrix

X(s) = \$(s) X(0) + \$\phi(s) \mathbb{B} B U(s)

y(t) = C x(t) => y(s) = C x(s)

y(s) = C (s) x(o) + \$\phi(s)\$ B U(s)]

y(s) = \frac{f.T}{2} y(t)

A controllability

= if system states change by changing system ilp.

Mc=(B AB AB--.. A-B) (system) JI

Dif |Mc| to system is controllable

2nd order = to Mc= (B AB)

3rd order = Mc=(B AB ÅB)

(5) observability

ر الخاله دی النظام یک (states) ومنت عاری نعملی) (estimation) النجام الفرج وعایز تعرف ما بداخل النظام فی الحاله دی النظام یک سری النظام فی الحاله دی النظام یک سری النظام دی النظام یک النظام دی النظام یک الن

XX In some cases, the states Couldn't be? measured for the following reasons:-1- the location for Physical states. 2- The measuring instruments are not valid. sif internal states can be calculated from observation of olf response to system is observable Dobservable Matrix M. $\mathcal{H}_{0} = \begin{vmatrix} C \\ CA \\ CA^{2} \\ \vdots \\ CA^{-1} \end{vmatrix} : |\mathcal{H}_{0}| \neq 0$ observable

Lec 10,11 34 =